

GCSE MARKING SCHEME

MATHEMATICS - LINEAR
NOVEMBER 2012

INTRODUCTION

The marking schemes which follow were those used by WJEC for the November 2012 examination in GCSE MATHEMATICS - LINEAR. They were finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conferences were held shortly after the papers were taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conferences was to ensure that the marking schemes were interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conferences, teachers may have different views on certain matters of detail or interpretation.

WJEC regrets that it cannot enter into any discussion or correspondence about these marking schemes.

PAPER 1 - FOUNDATION TIER

PAPER 1 (Non calculator) Foundation Tier	Marks	FINAL MARK SCHEME Comments
1. (a) (i) 6 583	B1	Comments
(ii) thirteen thousand four hundred and six	B1	
1. (b) 182	B1	
1. (c) 309	B1	
1. (d) 72	B1	
1. (e) (i) 8740 (ii) 8700	B1 B1	
1. (f) 1, 2, 4, 8, 16	B2	B1 for any 3 correct factors with at most 1 incorrect number. Allow 1×16, 2×8, 4×4 or repeats in a list.
2. (a) 8 thousand(s) OR 8000 OR thousand(s)	9 B1	D0 for 1000
2. (a) 8 thousand(s) OK 8000 OK thousand(s)	D1	<u>B0 for 1000</u>
2. (b) 81	B1	Accept 9×9 OR 9 ² , but 9 gets B0
2. (c) Tom spends £14 on cards Each pack costs (£)14/10	M1 M1	Allow this M1 only for (£)15/10. Unsupported (£)1.50 gets 0
= (£)1.4(0) OR 140 (p)	A1	C.A.O.
2. (d) 25 (%)	B1	1/4 OR .25 get B0.
2. (e) (74 OR 75 OR 74.6 OR 70 <u>OR 80</u>) × 100 = 7400 OR 7500 OR 7460 OR 7000 <u>OR 8000</u>	M1 A1	Good estimates F.T their estimates for simple calculations Answers only get M0, A0.
2. (f) 23	B1 9	Thiswers only get 1410, 710.
3. (a) Profit = $20 \times 24 - 150$	M1	Correctly substituted shown by correct attempt to evaluate.
= (£) 330	A1	Must show that the substitution is 20×24 then -150
3. (b) Outlay = $10 \times 24 - 180$	M1	For correct substitution with subtraction
$= (\pounds) 60$	A1 4	Allow embedded references to the correct answer.
4. (a) cone	B1	Circular based pyramid gets B0
octagon (square based) pyramid OR <u>rectagular based</u>	B1 B1	Triangular pyramid gets B0, but pyramid gets B1
4. (b) diameter	B1	
tangent	B1	
chord	B1	
4. (c) (i) All 3 lines of symmetry	B2	B1 any one of them and no incorrect lines OR 2 correct lines and up to 1 incorrect line.
(ii) BOTH lines of symmetry	B1 9	B0 if any incorrect lines are drawn
5. (a) Missing side segment = 6	S1	This may be implied by some correct methods
Perimeter = 10+2+10+2+10+6+10+2+10+2 = 64 (cm)	M1 A1	Attempt to add all sides of the shape C.A.O.
5. (b) Area = $3 \times 10 \times 2$	M1	OR equivalent
= 60	A1	C.A.O.
cm ²	U1	Independent of all other marks. Watch out as the area of the 'gap' is also 60.
	6	

PAPER 1 (Non calculator) Foundation Tier	Marks	FINAL MARK SCHEME Comments
6. Finding the costs per pupil of tickets, bus and lunch Cost of ticket per pupil = 915/98 = (OR 900/100) = (£)9 Cost of bus per pupil = 290/98 = (OR 300/100) = (£)3 Total cost per pupil = £9 + £3 + £3.95 = £15.95 = (£)16 (to nearest £)	M1 A1 M1 A1	Allow any method that implies estimating Allow unsupported answers in the range 7-11 incl. But if working shown then mark it. Allow any method that implies estimating Allow unsupported answers in the range 2-4 incl. But if working shown then mark it. F.T. if both Ms awarded Must be rounded to the nearest £
OR Finding the TOTAL cost of tickets, bus and lunches /98 Total cost of lunches = (£)3.95 × 98 = (OR £4 × 100) = (£)400 Total for the trip = $400 + 915 + 290 = (OR 400 + 900 + 300)$ = (£) 1600 Cost per pupil = (1605 OR 1600)/100 = (£)16 (to nearest £) NOTE: $98 \sim 100$ (£)3.95 \sim (£)4 (£)915 \sim (£) 900 (£)290 \sim (£)300	M1 A1 A1 M1 A1	Allow any method that implies estimating Allow estimated answers F.T. if M awarded Allow any method that implies estimating If no marks then SC1 for any 3 of these estimates
OWC Look for Spelling Clarity of text explanations The use of notation – watch for '=','£', 'p' being used appropriately. QWC2: Candidates will be expected to present work clearly, with words explaining their processes or steps AND make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer QWC1: Candidates will be expected to present work clearly, with words explaining their processes or steps OR make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer	QWC 2	QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar. QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar. OR Evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar. QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation and grammar.

PAPER 1 (Non calculator)	Mandan	FINAL MARK SCHEME
Foundation Tier	Marks	Comments
7. Toronto down 5	B1	If given as -5 then B0, but allow B1 if Moscow is given as -4
Glasgow –4 Moscow down 4 Reykjavik –7	B1 B1 B1 4	43 -4
8. (a) Overlay Plots Line	P1 L1	A valid attempt at drawing a line/curve through the points
8. (b) Any correct strategy, e.g. 2 times value at 20 kilometres per litre	M1	Any correct method using graph or table.
$56 \times 2 = 112$	A1 4	F.T. their graph. Unsupported answers in the range 108 – 116 <u>inclusive</u> get M1, A1.
9. (a) 5 3 (1 1) 3 1 (1 3) (1 1) 3 5 (1 3) 5 7	B2	B1 for at least 4 correct entries Negative numbers are errors in this table, but follow through, if needed in part (b)
(b) $\frac{7}{16}$ (of 320)	M1	F.T. their table. F.T. 'their 7/16' if a fraction less than 1 Sight of bone fide 140 in later working OR 140/320 gets
= 140	A1	M1, A1. Accept words '7 out of 16', or '70 out of 160' here.
Cost = 320×50 (p) OR Prizes = 140×80 (p) (£) 160 or 16000 (p) OR (£)112 or 11200 (p)	M1 A1	For either method and accuracy for cost OR prizes. F.T. 'their 140' provided it is clearly identifiable. A0 for £16000 OR 160p OR 112p OR £11200
320 × 50(p) – their 140 × 80 (p) = £48 OR 4800p	M1 A1	F.T. full method (ignore units for the M1). Rounded up or down figure if their 140 is not a whole number
10. (a) Base angle = 66	B1	x = 66 with no working gets B1M0A0
$ \begin{array}{cccc} & x = 180 - 66 - 66 \\ & = 48 \end{array} $	M1 A1	F.T. their 180 – 114
10. (b) (180 – 106) = 74	B1	For finding 4 th angle. Also look in their diagram. 74 on its own gets this B1, even as y = 74
360 – 114 – 53 – 74	M1	Angle sum of quadrilateral. Note that $180 - 167 + 106$ is equivalent $(114 + 53)$
= 119 (°)	A1 6	F.T. 'their 74'
11. A (9, 5)	B2	B1 for each ordinate
B (26, -4) C (21, -13)	B2 B2	B1 for each ordinate B1 for each ordinate. F.T. 'their B + (-5, -9)'
	6	

PAPER 1 (Non calculator)	Marks	FINAL MARK SCHEME
Foundation Tier		Comments
12.(a) (£)6400	B1	
(b) (£)2000	B1	Come weight about and come weight below
(c) Reasonable straight line of best fit	B1	Some points above and some points below
		Do not accept from 'corner' to 'corner' of the graph
(d) Negative (correlation)	B1	paper
(e) FT from a line of best fit (reading accurate to small	B1	OR an answer between (£)2600 and (£)3600 inclusive if
square) (curved line or straight line, not dot-to-dot)	D1	no line of best fit.
H1	5	
13. (a) 3(8x +1)	B1	CAO
(b) $x(x-6)$	B1	CAO
(c) $2x^4 + 12x$	B2	B1 for each term. If B2 penalise further wrong work -1.
(d) $x/3 = 25 - 15$	M1	Or alternate correct first step
x = 30	A1	CAO. Accept embedded answers. Mark final answer.
F13 parts (a) to (d) are H4 parts (b) to (e)		SC1 for $x=120$ from $x/3 = 40$, OR
() 7 7 9	D.1	SC1 for 'ladder method' showing -15, ×3
(e) $5x - 7 = 3x + 6$	B1	FT until 2 nd error
2x = 13 $x = 6.5 \text{ OR } 6\frac{1}{2}$	B1 B1	OR x = 13/2 Must be simplified.
X = 0.5 OR 0/2	9	Must be simplified SC1 for 'ladder method'
14.(a) Strategy, shorter edges meeting (accept a diagram)	S1	May be implied in later working that this is the
(Showing) 6 on longer sides (2 lots of 3) and 1 on each end	M1	arrangement
OR idea end tables seat 7 people and middle table seat 6 people	1411	diffungement
(Number of tables is) $(164 - 2) \div 6$	M1	Accept intention, not about notation
OR 2 correct trials with equivalent " $\times 6 + 2$ "	1,11	SC2 for 79 or SC1 for (164 - 6)/2
27 (tables)	A1	
		Alternative:
		Any 3 multiples of 6 shown or3 terms of a sequence
		going up in 6s, or 164/6 or 164÷6 S1
		$27 \times 6 = 162$ OR 27 remainder 2 OR 27.3(3) M1
		(this implies S1 also)
		$162 + 2 = 164 (seen or implied) \qquad M1$
		27 (tables) A1
		An answer of 27 from working '27 remainder 2' or '27.3(3)' must be confirmed in order to award the final
		M1, A1 (i.e. remainder justified), otherwise SC1 instead
		An answer of 27 (tables) without working is awarded SC3
		The answer of 27 (tables) mandal working is awaraca see
(b) $(n-2) \div 6$ OR $(n-2)/6$	В3	FT misunderstanding longer edges joined leading to
(b) (ii 2) (b) OR (ii 2)/(b)		$(n-6) \div 2$
		B2 for $n-2 \div 6$ or $n-2/6$ or $-2 \div 6$
		B1 for -2 or +6 in an expression
		or $n = 6 \times tables + 2$, or $n = 6 \times t + 2$
Н5	7	$B0 \text{ for } \times 6 + 2 \text{ or } n \times 6 + 2$
15. Realising could be 2+2, 1+3, 3+1	B1	May be within a sample space diagram, e.g. sight of two-
, -,-		way table with three 4s shown, or the appropriate additions
		, 11 1
Realising 36 different outcomes OR sight of $1/6 \times 1/6$	B1	Maybe shown in a sample space diagram with
OR product of 2 terms both with denominators of 6 seen		indication of 36, must be stated not implied
OR sight of a denominator of 36	_	
3/36 or equivalent	B1	
<u>H6</u>	3	Ignore incorrect cancelling
16.	D.1	If boxes are blank, mark the working
Middle card 6	B1	Smaller numbers to one side and larger to the other
Two cards (or three cards) 3 <u>as the mode for their cards</u> First card 1 and last card 9 (or in reverse)	B1 B1	3 is the distinct mode for their cards OP any pair of single digit numbers (including
First card 1 and last card 9 (or in reverse)	DI	OR any pair of single digit numbers (including negatives) with a difference of 8
Correct answer 1 3 3 6 7 8 9 or in reverse	B1	CAO
H7	4	
	1 7	1

PAPER 1 - HIGHER TIER

PAPER 1 Higher Tier	Marks	FINAL MARK SCHEME Comments
1.(a) (£)6400	B1	
(b) (£)2000	B1	
(c) Reasonable straight line of best fit	B1	Some points above and some points below.
		Do not accept from 'corner' to 'corner' of the graph paper
(d) Negative (correlation)	B1	
(e) FT from a 'line of best fit' (reading accurate to small	B1	OR an answer between (£)2600 and (£)3600 inclusive if no
square) (curved line or straight line, not dot-to-dot)	5	line of best fit.
2.(a) Correct translation	B1	
(b) Correct reflection	B2	B1 for sight of $y = 6$ or reflection in any horizontal
3.(a)	3	Mark intention of straight lines throughout the question
[3.(a)		Use the acetate to follow through for each time period, i.e.
		8:15, 9:00,11:00
		Penalise not joined with lines -1 only
(08:00, 0) to (08:15, 2.5) joined with a line	B1	1 change not joined with mice 1 chily
(**************************************		
(08:15, 2.5) to (08:36, 2.5) joined with a line AND	B1	
(08:36, 2.5) to (09:00, 5.5) joined with a line		
(09:00, 5.5) to (11:00, 5.5) joined with a line	B1	
(11.00.5.5) (11.20.0) (11.11.11.11	D.1	6026 6 4 1 11 4 1 1 1 1
(11:00,5.5) to (11:30, 0) joined with a line	B1	SC2 for an 'correctly shaped but inverted travel graph', or SC1 if '1 error' in this inverted travel graph
(b) $5.5 / 30$ (minutes) or $5.5 / \frac{1}{2}$ (hour) or $5.5 + 5.5$	M1	Accept 5 ½ for the distance
11/60(miles/min)	IVII	FT their total distance from their graph in (a), but time must
11/00(miles/mill)		be 30 minutes or ½ hour, do not accept 0.30 as 30 minutes
11 (mph)	A1	or /2 mour, do not accept one as so minutes
	6	
4.(a) 6x - 2x = 21 + 7	B1	FT until 2 nd error
4x = 28	B1	OR $x = 28/4$
x = 7	B1	Must be simplified
(b) $3(8x + 1)$	B1	CAO
(c) $x(x-6)$	B1	CAO
$(d) 2x^4 + 12x$	B2	B1 for each term. If B2 penalise further incorrect work -1
(e) $x/3 = 25 - 15$ x = 30	M1 A1	Or alternate correct first step
x = 30	AI	CAO. Accept embedded answers. Mark final answer. SC1 for x=120 from x/3 = 40, OR
	9	SC1 for 'ladder method' showing -15, ×3
	7	SCI for fadder friction showing -13, 5

PAPER 1		FINAL MARK SCHEME
Higher Tier	Marks	Comments
5.(a) Strategy, shorter edges meeting (accept a diagram) (Showing) 6 on longer sides (2 lots of 3) and 1 on each end	S1 M1	May be implied in later working that this is the arrangement
OR idea end tables seat 7 people and middle table seat 6 people (Number of tables is) $(164-2) \div 6$ OR 2 correct trials with equivalent " $\times 6 + 2$ " 27 (tables)	M1 A1	Accept intention, not about notation. For a complete correct method that could lead to 27 tables
		SC2 for 79 or 54, or SC1 for (164 – 6)/2
		Alternative: Any 3 multiples of 6 shown or3 terms of a sequence going up in 6s, or $164/6$ or $164+6$ S1 $27\times6=162$ OR 27 remainder 2 OR 27.3(3) M1 (this implies S1 also) $162+2=164$ (seen or implied) M1 27 (tables)
		An answer of 27 from working '27 remainder 2' or '27.3(3)' must be confirmed in order to award the final M1, A1 (i.e. remainder justified), otherwise SC1 instead
QWC0 for answer only	QWC	An answer of 27 (tables) without working is awarded SC3
QWC2: Candidates will be expected to • present work clearly, maybe with diagrams and words explaining process or steps AND	2	QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.
 make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer 		QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar OR
QWC1: Candidates will be expected to • present work clearly, maybe with diagrams and words explaining process or steps		evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar.
make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer		QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation or grammar.
(b) $(n-2)\div 6$ OR $(n-2)/6$ OR equivalent	В3	FT misunderstanding longer edges joined leading to (n-6)÷2
	9	B2 for n-2 ÷6 or n - 2/6 or -2 ÷ 6 B1 for -2 or ÷6 in an expression or n = 6×tables + 2, or n = 6×t + 2 B0 for ×6 + 2 or n×6 + 2
6. Realising could be 2+2, 1+3, 3+1	B1	May be within a sample space diagram, e.g. sight of two- way table with three 4s shown, or the appropriate additions
Realising 36 different outcomes OR sight of 1/6 ×1/6 OR product of 2 terms both with denominators of 6 seen OR sight of a denominator of 36	В1	Maybe shown in a sample space diagram with indication of 36, must be stated not implied
3/36 or equivalent	B1 3	Ignore incorrect cancelling

PAPER 1		FINAL MARK SCHEME
Higher Tier	Marks	Comments
7.		If boxes are blank, mark the working
Middle card 6	B1	Smaller numbers to one side and larger to the other
Two cards (or more) 3 as the mode for their cards	B1	3 is the distinct mode for their cards
First card 1 and last card 9 (or in reverse)	B1	OR any pair of single digit numbers (including negatives)
		with a difference of 8
Correct answer 1 3 3 6 7 8 9 or in reverse	B1	CAO
0 (-) 2	4 M1	N-4 -11 21 4- h- 1:66444
8.(a) 3 reasonable rounded values which could lead to simple calculations	M1	Not all 3 need to be different to those given
Correct evaluation for their figures	A1	(Common responses include 5 here)
(b) 3.45	B1	CAO
(c) 3/16	B1	Allow 0.1875. Do not accept 1.5/8
(d) 2, 2, 2, 2, 3, 5	B2	B1 for at least 2 correct primes before 2 nd error
$2^4 \times 3 \times 5$	B1	FT "their" primes, needs to have at least 1 index>1
(e) 1/0.9 or 1/(9/10) or 10/9	M1	
10/9 and indication that this is GREATER than 0.9	A1	Or $1^{1}_{/9}$ or 1.1(11), statement in reverse
0() (2 15 0 20	9	D16
9.(a) $6x^2 + 15x - 8x - 20$ = $6x^2 + 7x - 20$	B2 B1	B1 for any 3 terms correct FT from B1 provided collection required. Mark final
-0x + /x - 20	101	answer
(b) $(2x+3)(x-1)$	B2	SC1 for an answer of $6x^2() - 20$
Both possible solutions $x = -3/2$ AND $x = 1$	B1	B1 for (2x 3)(x 1) or (2x 1)(x 3)
(c) $(x + 5)^6$	B1	FT from their pair of brackets
(d) n ² + 4 or equivalent	B2	CAO. Mark final answer
	9	B1 for $(1)n^2 \pm$, not for n^2 alone
10.(a) All entries correct	B2	B1 for any one pair of branches correct
(b) 0.7×0.7	M1	FT from their tree, provided numbers >0 and <1
0.49	A1	
	4	
11.(a) Initial strategy, e.g. sketch of concentric rectangles	S1	
Correct method to find area, e.g. subtraction of areas or	M1	For intention, but some sections may be missed
composite shapes $(9+2x)(5+2x) - 9 \times 5$ or $9x+9x+5x+5x+x^2+x^2+x^2+x^2$	A1	Or equivalent
$(9+2x)(3+2x) - 9\times 3$ or $9x+9x+3x+3x+x+x+x+x+x+x+x+x+x+x+x+x+x+x+$	A1	Mark final answer
TA 120A 01 T(A 1 /A) 01 TA(A 1 /)	111	If the path has been built inside then MR-1 and FT (leading
		$to 28x - 4x^2$
(b) Strategy, drawing with ¼ circles in corners	S1	FT from (a), to give their (a) $-4x^2 + \Pi x^2$,
OR sight of πx^2 of a fraction or multiple of πx^2		Not for sight of πr^2
(or equivalent)	3.61	
$9x+9x+5x+5x+4 \times 1/4 \times \Pi \times x^2$	M1 A1	Mork final anguar
$28x + \Pi x^2$ or $x(28 + \Pi x)$	7	Mark final answer If the path has been built inside then MR-1 and FT
12.(a) -5 and -12	B2	B1 for each correct answer
(b) Any 6 correct plots	B2 B1	FT from (a)
All 8 correct plots joined with a smooth curve	B1	FT from (a)
(c) 2 and 6	B1	Coordinate notation is not required.
		Accept embedded answers
(d) y values 0, 3, 4, 3, 0	B1	Sight of these values alone or within a calculation
Split correct region into areas to sum	M1	FT for 1 incorrect y value only.
		May included area below x-axis
Numerically correct area calculations shown	A1	$(\frac{1}{2}(3) + \frac{1}{2}(3+4) + \frac{1}{2}(4+3) + \frac{1}{2}(3))$
10 ((+ 60 if below x-axis included
10 (square units)	A1 9	CAO
13. $y \alpha 1/x^2 \text{ OR } y = k/x^2$	B1	Ignore use of incorrect symbol 'α' later
15. $y \in 1/X$ OR $y = k/X$ $10 = k/12^2$	M1	FT y α 1/x or y α x ² for possible M1, A1
$y = 1440/x^2$	A1	11 y w 1/A of y w A for possible wit, At
j = 1110/A	3	

PAPER 1 Higher Tier	Marks	FINAL MARK SCHEME Comments
14.(a) Transformation horizontally to the right	B1	
Correct translation with 2 indicated correctly on the x-axis	B1	SC1 for left shift with -2 indicated on the x-axis
(b) Idea of reflection in x-axis	B1	May include an incorrect translation, but clearly there has
		been a reflection
Idea of vertical translation	B1	Allow 'up' or 'down'
Correct transformation with 3 indicated on the y-axis	B1	1
	5	
15.(a) 1/8000	B2	B1 for 1/20 ³
(b) Attempt to subtract $100x = 65.252$ and $x = 0.652$	M1	Or equivalent for $1000x - 10x$
646/990 ISW	A1	Final answer of 64.6/99 M1 only
(c) $9 - 15\sqrt{2} - 15\sqrt{2} + 50$	M1	With at least 3 of the terms correct OR $9 \pm a\sqrt{2} + 50$ with
$= 59 - 30\sqrt{2}$	A1	a≠0
Irrational	B1	CAO
	7	FT provided at least M1 awarded
16.(a) Any one correct area	B1	10, 15, 35, 80, 60
10 + 15 + 35 + 80	M1	
= 140	A1	If no other marks allow SC1 for an answer of 135
(b) (i) 50 (seconds)	B1	Do not accept a group or interval
(ii) Correct histogram	В3	B2 for sight of 1, 2, 2.5, 3.5, 10 or histogram with first bar
		correct but with 1 error in one of the other bars, OR
		B1 for histogram with any 3 bars correct
(c) A reasonable statement,	E1	Could be either Yes or No with a suitable reason.
e.g. 'No, children median lower', or 'no, 140 children less		FT their histogram
than 50 seconds but only 100 adults', or 'no, because more		Accept an answer of 'same' if the candidate calculating the
adults spent over 50 seconds'	8	means to be the same

PAPER 2 - FOUNDATION TIER

PAPER 2 (Calculator allowed) Foundation Tier	Marks	FINAL MARK SCHEME Comments
1. (a) (242.68) 146.16 (tables) 87.5(0) (chairs) 160.56 (cabinets)	B1 B1 B1	
(£) 636.9(0)	B1	F.T. their figures for 1 error
(b) Builder pays (£) 573.21	B2	F.T. their total rounded or truncated. Must be in 2 dec. places for the B2 B1 for a correct 10% (£) 63.69. 2 dec. pl. NOT required for B1
	6	
2. 50g 500kg 50mg 50kg	B1	
27 litres (270 ml) 2.7 cm ³ 270 litres	B1	
180cm 18m 1800cm	B1	
266mm 266cm 266km (266km)	B1	
	4	
3. (a) Evidence of square counting 72 – 78 (inclusive)	M1 A1	
3. (b) Lines Arc	B1 B1	Correct curvature starting and ending at the candidate's 2 lines.
3. (c) c	B1	If angle values used then they must be appropriate on
a b	B1 B1	the diagram AND in the correct place on the answer line.
	-	
4. (a) Spring (S) 10, Summer (U) 15, Autumn (A) 8,	7 B2	May be inferred from their bar chart.
Winter (W) 7		B1 for any two/three correct frequencies
Both axes labelled, e.g. frequency along one axis and	B2	If frequencies score 0, then give B1 for all 4 correct tallies. B1 if no scale, but allow one square to represent 1
Spring (S), Summer (U), Autumn (A), Winter (W) along	B2	OR B1 if not labelled as 'frequency' or similar.
other axis (or on the bars)		If frequency scale starts with 1 at the top of the first square
Anywhere within the base (inc.) of the corres. bar. and uniform scale for the frequency axis starting at 0 and		the starting at 0 will be implied for this axis. Condone frequency numbers alongside square instead of
labelled 'frequency' OR 'number of pupils'.		at the top of the squares.
Four bars at correct heights (bars must be of equal width). Can be in any order.	B2	F.T. their frequencies throughout. B1 for any 2 or 3 correct bars on F.T. If no frequencies given in their working, penalise -1 for each incorrect frequency on their bars up to -4 (First and
(b) Summer OR U	B1	third B2s) Accept 15 and (Summer OR U), but B0 for 15 only
(c) 7/40 I.S.W.	B2	B1 for the 7 (in a fraction < 1) OR B1 for a denominator of 'their 40' (in a fraction < 1). F.T. their frequencies. Penalise –1 for incorrect notation, e.g. '7 out of 40', '7:40' Allow decimals and percentages including on F.T. For example, (0).175 or 17.5% for 7/40

PAPER 2 (Calculator allowed) Foundation Tier	Marks	FINAL MARK SCHEME Comments
5. (a) C A B O 1	B1 B1 B1	A should be between ½ and ¾ (Accept P for A). A should be to the right of the halfway and up to alongside the gap between the a and 1 in ball (OR between ê and 1 in pêl in the Welsh version) B should be at 1. C should be between 0 and ¼ (Accept G for C). C should be to the right of the 0 and up to alongside the y in probability (OR the y in tebygolrwydd in the Welsh version)
6. (¼) (0).25 (25%) any fraction equiv. to 6/10 (0.6) 60(%) any fraction equiv. to 3/4 (0.75) (75%)	4 B1 B1, B1 B1	ISW for the fractions 6/10 and 3/4 Do not accept fractions like 7.5/10
All triangles must be 'base' side to 'base' side 7. (a) Rhombus OR square Sketch	B1 B1	Mark name first then sketch B0 for what looks more like a parallelogram than rhombus
7. (b) Kite Sketch	B1 B1	Mark name first then sketch
8. (a) (i) Decrease previous term by 7 (ii) Multiply previous term by -2	4 B1 B1	Accept -7 . B0 for $n - 7$ Accept $\times -2$ B0 for $n \times -2$
8. (b) (i) 10w (ii) x - 6 and x + 6	B1 B1	Allow 10×w, w×10 and w10. Ignore any g(rams) Ignore w= and =w For both
8. (c) $1/9 \times 45 = 5$ and 4×5 = 20	M1 A1	Any correct method
8. (d) $5\times4 = 2P + 3\times-4$ 2P = 20 + 12 OR 32 P = 16	B1 B1 B1	Correct substitution, not awarded until the 2 multiplications are seen to be implemented. Sight of 20 and -12 gets B1 F.T. P= 32/2 gets B0. Must be 16 F.T. P = 'their 32'/2. Allow embedded answers, such as 20 = 2×16 - 12.
8. (e) $4x = 18$ ($x =) 4 \frac{1}{2}$ OR 4.5	B1 B1	Must be 18 NOT 21–3 (x=) 18/4 gets B0. (x=) 9/2 gets B0
9. (a) yuan = 700 × 9.79 = 6853 (yuan) <u>ISW</u>	11 M1 A1	Yuan not required but A0 for £6853
9. (b) Pounds = 2447.5/9.79 = (£) 250 <u>ISW</u>	M1 A1	£ not required but A0 for 250 yuan

PAPER 2 (Calculator allowed) Foundation Tier	Marks	FINAL MARK SCHEME Comments
10. (a) (10) 17 24 31 (b) (35 31) 27 23 19 (c) (Yes) because 100 is 60 away and 60 is divisible by 6 (d) After 5 steps 75	B1 B1 E2 B1 B1	E2 for 6×10 + 40 OR equivalent, <u>e.g. Yes, in 10 steps (E2)</u> E1 for considering 60 with an indication of steps of 6 e.g. listing all numbers between 40 to 100. 75 can be answered in lists, but the 5 must be given as an <u>answer</u> .
(e) Starting numbers are 44 apart.	B1	Allow <u>B1</u> for sight of 44 <u>OR 40 by comparing 21 and 61</u> after one step etc.
44 is divisible by 4	B1	SC1 for only listing the correct sequences.
11. (a) $(\hat{ACB}) = 60$ (°)	8 B1	Look for the angles shown in their diagram (Angles of an equilateral triangle are 60°)
$(B\hat{C}E) = 45 (^{\circ})$ $(A\hat{C}E) = 105 (^{\circ})$	B1 B1	(Half the angle of a square is 45°) C.A.O.
11. (a) (continued) QWC Look for Spelling Clarity of text explanations Some geometrical statements, e.g. angles of a equilateral triangle are 60° QWC2: Candidates will be expected to present work clearly, with words explaining their processes or steps AND make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer QWC1: Candidates will be expected to present work clearly, with words explaining their processes or steps OR make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer	QWC 2	QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar. QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar. OR Evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar. QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling
11. (b) First arcs Final arcs and line 11. (c) First arcs Final arcs and line	B1 B1 B1 B1	If no pair of compasses used (i.e no arcs) then 0 for their work in (b) and (c) They can use the points A and B for this first B1 Remember the 2 methods discussed in the conference.
Use Overlay 12. Bearing from Holyhead Bearing from Cardigan Position of Ship	9 M1 M1 A1	Use Overlay Within ±2°. Watch out for unambiguous 'dots' within Within ±2° the boundaries of the overlay and award M1s F.T. provided at least M1 One unambiguous 'dot' within the 'box' on the overlay gets all 3 marks.

PAPER 2 (Calculator allowed) Foundation Tier	Marks	FINAL MARK SCHEME Comments
13. One correct evaluation (1 dec.pl.) of x^3 –7x–2 $2 \le x \le 3$ Watch for pupils who are trying to make x^3 –7x equal to 2 rather than x^3 –7x–2 equal to 0.	B1	Calculations should be accurate to 1 decimal place rounded or truncated If no calculations are given accept use of "too low" or "too high" OR >0 and <0.
Two correct evaluations (1 dec.pl.) x^3-7x-2 $2.65 \le x \le 2.85$	B1	Useful Data
which give opposite signs for $f(x)$. Two correct (OR F.T.) evaluations (1 dec.pl.) $2.75 \le x \le 2.85$ which give opposite signs for $f(x)$.	M1	2 -8 2.1 -7.4390 2.2 -6.7520 2.3 -5.9330 2.4 -4.9760 2.7 -1.217 2.65 -1.9404 2.66 -1.7989 2.67 -1.6558 2.73 -0.763583 2.68 -1.5112 2.74 -0.609176 2.69 -1.3649
Thus solution is 2.8 correct to 1 decimal place. Note that candidates must give a method that proves the solution is 2.8 correct to 1 decimal place. Just stating 0.3520 is closer than -1.217 is NOT enough	A1 4	2.5 -3.8750 2.75 -0.453125 2.8 0.3520 2.6 -2.6240 2.76 -0.295424 2.81 0.5180 2.7 -1.2170 2.77 -0.136067 2.82 0.6858 2.8 0.3520 2.78 0.024952 2.83 0.8552 2.9 2.0890 2.79 0.187639 2.84 1.0263 3 4 2.8 0.352 2.85 1.1991
14.(a) 23 (m) (b) (12+24)÷4 9 (car lengths) (c)	B1 M1 A1	
Speed mph km/ h 30 48 70 112	M1 A2	Evidence of a method, e.g. ÷5 and ×8, or ×5 and ÷8 as appropriate, or sight of a correct scale, e.g. $80 \times 30 / 50$ A1 for either answer correct. Also implies M1
(d) 15 + 0.30 × 15 OR 38 + 0.20 × 38 or equivalents 19.5 and 45.6 65(.1 m)	M1 A2 A1	A1 for either correct answer. Accept 20 and 46 FT from M1, A1 FT from rounding to 'their 20'+ 'their 46 '= 66(m) Unsupported 65 or 66 gain full credit If no marks, award SC1 for an answer of 12.1 or 12 (giving the increase not the total).
15. 654 a	B1	Accept truncated or
173.31 b c c 10.18(8) d e	B1 B1 B1 B1	F.T. $a \times 0.265$ rounded answers F.T. $b + 30.45$ F.T. $c \times 0.05$ B0 if 105% given here F.T. $c + d - 42.36$
20.91(2) CR	B1	F.T. $ e - 192.50 $ Allow $\pm 2p$
Answers in the bill take precedence over answers on the 'working lines' below it.	6	If their total cost is < 192.50 then their final balance must show $-$ or CR. If their total cost is > 192.50 then B0.
16. (a) Area = $\frac{1}{2} \times 8.6 \times 4.1$ 17.6(3 cm ²) (b) (AB ² =) 8.6 ² + 4.1 ² OR 73.96 + 16.81	M1 A1 M1	Correct substitution in Pythagoras' Theorem
$(AB^2 =) 90.77$ (AB) = 9.5(273) (cm)	A1 A1	This work could be seen in (a) and should be credited appropriately.
Perimeter = 12.7 + 9.5 = 22.2 (cm) = 22 (cm)	M1 A1	FT their 8.6+4.1+ 'their AB if from Pythagoras work' Given to 2 sig. figs.
	7	

PAPER 2 - HIGHER TIER

PAPER 2		FINAL MARK SCHEME
Higher Tier	Marks	Comments
1. a = 76(°)	B1	
b = 53(°)	B1	
$c = 51(^{\circ})$	B1	FT 180 - (a + b)
2 () 22 ()	3	
2.(a) 23 (m)	B1 M1	
(b) (12+24)÷4 9 (car lengths)	A1	
(c)		
Speed	M1	Evidence of a method, e.g. ÷5 and ×8, or ×5 and ÷8 as
mph km/h 30 48	1411	appropriate, or sight of a correct scale, e.g. $80 \times 30/50$
	A2	A1 for either answer correct. Also implies M1
70 112		_
(d) $15 + 0.30 \times 15$ OR $38 + 0.20 \times 38$ or equivalents	M1	
19.5 and 45.6	A2	A1 for either correct answer. Accept 20 and 46
65(.1 m)	A1	FT from M1, A1
		FT from rounding to 'their 20'+ 'their 46 '= 66(m) Unsupported 65 or 66 gain full credit
		If no marks, SC1 for an answer of 12.1 or 12 (giving the
	10	increase not the total)
3.(a) Scale factor 2 enlargement	B1	
(Intention of the) Correct position	B1	Perhaps watch for the position of the bottom left vertex
(b) Correct rotation about (2, 1)	B2	B1 for rotation of 180° about (1, 2)
4. Janie 450/1.57 or Ami 30000/129.82	4 M1	
Janie (£)286.6242 or (£)286.62	A1	Allow (£)286.6(0)
Ami (£)231.0892 or (£)231.08 or (£)231.09 or (£)231	A1	Allow (£)231.1(0)
(£)186.62 and 131.09	B1	FT correctly subtracting (£)100 from each of their amounts,
	3.61	but not from 450 or 30000
Sight of an amount (not starting dollars or yen) × 1.18 669.9(0 euros) or 669 (euros) or 670 (euros)	M1 A1	For method of conversion, even if £250 not added FT their (amounts in £s) rounded or truncated, e.g. leading
009.9(0 euros) or 009 (euros) or 070 (euros)	AI	to 669.88. Must be FT for the 3 girls e.g. {186. ()+
Look for		131.() + 250 × 1.18 correctly evaluated, rounded or
• spelling		truncated
 clarity of text explanations, 	QWC	
• the use of notation (watch for the use of '=', £,	2	MR-1 for treat situation of exchange of money for whole
\$, Yen being appropriate)		notes
QWC2: Candidates will be expected to		QWC2 Presents relevant material in a coherent and logical
present work clearly, with words explaining		manner, using acceptable mathematical form, and with few
process or steps		if any errors in spelling, punctuation and grammar.
AND		OWOLD LINE
make few if any mistakes in mathematical form,		QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form,
spelling, punctuation and grammar and include		spelling, punctuation or grammar
units in their final answer		OR
QWC1: Candidates will be expected to		evident weaknesses in organisation of material but using
present work clearly, with words explaining		acceptable mathematical form, with few if any errors in
process or steps		spelling, punctuation and grammar.
OR		QWC0 Evident weaknesses in organisation of material, and
make few if any mistakes in mathematical form,		errors in use of mathematical form, spelling, punctuation or
spelling, punctuation and grammar and include	8	grammar.
units in their final answer		<u> ~ </u>

PAPER 2	Marks	FINAL MARK SCHEME
Higher Tier		Comments
5.(a) 7.6 (cm)	B1	
(b)(i) Mid-points 5,6,7,8,9 $5\times4 + 6\times2 + 7\times1 + 8\times1 + 9\times2$	B1 M1	FT their mid points including bounds provided they fall
3^4 + 0^2 + 7^1 + 8^1 + 9^2	IVI 1	within the classes. $20 + 12 + 7 + 8 + 18 = 65$
Intention their $\sum fx / 10$	m1	Willing the classes. 20 + 12 + 7 + 0 + 10 (= 03)
6.5 (cm)	A1	(65/10) For correct evaluation of $\sum fx / 10$
(ii) Modal class $4.5 \le s < 5.5$	B1	Accept '4.5 to 5.5'
$Median 5.5 \le s < 6.5$	B1	Accept '5.5 to 6.5'
6.(a) Radius 2.3	7 B1	
$\Pi \times 2.3^2 \times 8.4$	M1	
139.5(998 cm ³) to 139.7(cm ³)	A1	Do not accept from premature approximate
		SC1 for an answers 558(.3992 cm ³) to 558.7(cm ³)
(b)(i) $(x^2 =)3.4^2 + 5.6^2$	M1	
$x^2 = 42.92 \text{ or } x = \sqrt{42.92}$ 6.6 (cm)	A1 A2	Depends on previous M1 and process of √. Mark final
0.0 (CIII)	AZ	answer.
		A1 for 6.5(51 cm)
$(ii) \frac{1}{2} \times 5.6 \times 3.4$	M1	
$9.5(2 \text{ cm}^2)$	A1	Mark final answer
7.(a) Correct frequency polygon	9 B2	Must be accurate between bounds of 1 small square
7.(a) Correct frequency polygon	D2	horizontally and on the line vertically
		B1 if translated OR joined with curve or not joined OR one
		plot incorrect within the polygon
		Ignore frequency diagram as working
(b) 22 60 90 100	B1	
(c) Uniform scale vertically Plotting all points at the upper bounds	B1 B2	Appropriate for their values in (b) FT their <u>cumulative</u> table only if cumulative
Trotting an points at the upper bounds	D2	Ignore if (50, 0) omitted
		Must be accurate on vertical lines and horizontal lines
		B1 if one error in plots, OR for all vertical plots correct but
	D.1	not at upper bounds
All 6 accurate upper bound plots joined with a curve or lines	B1	FT from their <u>cumulative</u> graph in (d)(i) and (ii)
(d)(i) Median for their graph	B1	(Answer in the range 63.5 to 64 (cm))
(G)(I) INTEGRAL TOT WICH GRAPH	21	(67 to 68 - 60 to 60.5)
(ii) Idea UQ – LQ, with an attempt at readings and	M1	
intention to subtract	, ,	
Interquartile range accurate for their graph	A1	(Answers in the range 6.5 to 7.5)
8.(a)(i)	10	
45.5 46.5	B2	B1 for any 3 correct entries
54.5 55.5		Accept .49* RECURRING as being equivalent to .5
61.5 62.5	F.*	
(ii) 161296(.875 cm ³) or 161297 (cm ³) ISW	B2	FT their greatest provided all > given values and <47, <56 and <63 respectively
		B1 for selection of 46.5 (×) 55.5 (×) 62.5 (sight of digits
		161296 or 161297). Allow SC1 for an answer of 164.5, or
		for selecting and recording addition for their greatest values
(b) Least: (x-0.5)(y-0.5)(z-0.5)	B2	B1 for minor slip, or omission of brackets, there needs to be
		intention to multiply, or if further incorrect working
	6	B0 for sight of the 3 terms only without intention to multiply
9. $\tan A = 3.2/7$	M1	murupiy
24.567(°) rounded or truncated	A2	A1 for 0.457 or tan ⁻¹ 3.2/7
		SC1 for calculating B , an answer of 65.43(°),
	3	this is not for an answer labelled as A

PAPER 2	35.1	FINAL MARK SCHEME
Higher Tier	Marks	Comments
10.(a) Method, equating coefficients or alternative	M1	Allow 1 slip, but not in equated coeffs.
First variable correct	A1	$x = 11 \ y = -3$
Method to find second variable	M1	FT their first variable
Second variable correct	A1	
(b) $11(3 + x) + 2(2x - 1) = 13 \times 2 \times 11$	M2	No M mark if left as quotient
		M1 for 2 of these 3 terms correct
15x + 31 = 286	A1	FT from M1 for A1 only
x = 17	A1	CAO (Must be simplified)
(c) 7r - ar = b - c	B1	Like terms FT until second error
r(7-a) = b - c	B1	Factorise
r = (b - c)/(7 - a) or equivalent	B1	Isolate
	11	
11.(a) 0.05	B1	Accept equivalents, 1/20
(b) 1.1×10^{-4}	B2	B1 for 1×10^{-4} or 1.11×10^{-4} or 1.111×10^{-4}
		SC1 FT from their (a)/450 correctly expressed in standard
	3	form
12.(a) $(y =) 360 - 2x$ or $(y =) 2(180 - x)$ ISW	B2	B1 for appropriate $2x$, or $180 - x$ may be seen on the
		diagram or labelled, OR B1 for $x = (360 - y)/2$, or a correct
		expression but not 'y='
(b) FGH = 90° seen or implied by used in calculation	B1	
$FH = 6.8/\sin 32 \text{ (}\times\sin \text{FGH)}$	M2	M1 for $\sin 32 = 6.8$ / FH or FH/ \sin FGH = 6.8/ $\sin 32$
FH = 12.8(32 cm) or 13 (cm)	A1	Answer of 12 gets A0
	6	
13.		Accept descriptions
'Three sides' or SSS	B1	Do not accept e.g. 'dashes in the same places'
'Two sides and INCLUDED angle' or SAS	B1	Must be clear that it is the included angle
	2	
14. Strategy to find (½) PQ and <pbq< td=""><td>S1</td><td></td></pbq<>	S1	
$PQ^2 = 4^2 + 6^2 - 2.4.6.\cos 82$	M1	
$PQ^2 = 45.31969$	A1	M 1 1 11 1
PQ = 6.73199 $PQ^2 = 8^2 + 8^2 - 2.8.8.CosPBQ$	A1	Maybe embedded
$PQ = 8 + 8 - 2.8.8.COSPBQ$ $Cos PBO = 9^2 + 9^2 - PO^2$	M1 A1	OR Alternative: $\sin \frac{1}{2} PBQ = \frac{1}{2} PQ / 8$ M1 $< \frac{1}{2} PBQ = \frac{24.88}{2}$ A1
$\cos PBQ = \frac{8^2 + 8^2 - PQ^2}{2.8.8}$	AI	~
2.8.8 <pbq 49.763(°)<="" =="" td=""><td>A1</td><td>PBQ = 49.763(°) A1</td></pbq>	A1	PBQ = 49.763(°) A1
<pbq 03(*)<="" 49.="" =="" td=""><td>AI</td><td>Accept answers in the range 49.5 to 49.8 inclusive, or 50</td></pbq>	AI	Accept answers in the range 49.5 to 49.8 inclusive, or 50
A	M1	Correct answer, not FT FT their <pbq 82="" all="" and="" awarded<="" m="" marks="" not="" provided="" td=""></pbq>
Area shaded = $(\langle PBQ/360 \rangle) \times \Pi \times 8^2$ = 27.79 (cm ²) or 28 (cm ²) or 27.8(cm ²)		Accept answers in the range 27.6 to 28 inclusive
- 21.17 (CIII) OF 28 (CIII) OF 21.8(CIII)	A1 9	Accept answers in the range 27.0 to 26 inclusive
15.(a) Decision to find overall totals of a, e, r and number	M1	(34 and 132)
of letters	1011	(34 and 132)
34/132 or 0.2575 or equivalent	A1	Mark final answer
5-1/132 of 0.2373 of equivalent	111	Wark findi diiswoi
(b)Use or sight of (a, e, r =) 34 AND (number of letters =)	B1	Accept sight of 34 and 132, or 17 and 66. FT from (a)
132, OR, sight of any correct probability product,	"	For the idea without need to use values
equivalent to/132×/131 (or/66×/65) as		(As $66 = 132 \div 2$)
appropriate	S1	· · · · · · · · · · · · · · · · · · ·
P(at least one of a,e,r) = $1 - P(\text{none})$		
OR equivalent full strategy	M1	FT their totals, a method that would lead to correct answer
$1 - 98/132 \times 97/131$ or equivalent full method	A2	A1 for answer not correct to 2dp, as a result of incorrect or
0.45		premature rounding
	7	N.B. Markers check working for no replacement
16. Cosine curve from 0° to 360°	M1	Any vertical translation, but must be correct horizontally
		Accept if numbers of degrees missed but unambiguous
Correct cosine curve with the correct translation, with 2	A1	
marked on the y-axis	2	

GCSE Mathematics - Linear MS November 2012/ED



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