

Solutions

Surname	Centre Number	Candidate Number
Other Names		0



**GCSE – NEW**

3300U30-1



**MATHEMATICS**  
**UNIT 1: NON-CALCULATOR**  
**INTERMEDIATE TIER**

E      D      C      B  
 30    49    76    106  
 ---  
 15+   25+   38+   53+

**TUESDAY, 8 NOVEMBER 2016 – MORNING**

**1 hour 45 minutes**

**ADDITIONAL MATERIALS**

The use of a calculator is not permitted in this examination.  
 A ruler, protractor and a pair of compasses may be required.

**INSTRUCTIONS TO CANDIDATES**

Use black ink or black ball-point pen. Do not use gel pen or correction fluid.

You may use a pencil for graphs and diagrams only.

Write your name, centre number and candidate number in the spaces at the top of this page.

Answer **all** the questions in the spaces provided.

If you run out of space, use the continuation page at the back of the booklet, taking care to number the question(s) correctly.

Take  $\pi$  as 3.14.

**INFORMATION FOR CANDIDATES**

You should give details of your method of solution when appropriate.

Unless stated, diagrams are not drawn to scale.

Scale drawing solutions will not be acceptable where you are asked to calculate.

The number of marks is given in brackets at the end of each question or part-question.

In question 6, the assessment will take into account the quality of your linguistic and mathematical organisation, communication and accuracy in writing.

For Examiner's use only		
Question	Maximum Mark	Mark Awarded
1.	6	6
2.	3	9
3.	3	12
4.	6	18
5.	5	27
6.	7	30
7.	5	35
8.	3	38
9.	3	41
10.	6	47
11.	7	54
12.	3	57
13.	4	61
14.	4	65
15.	5	70
16.	6	76
17.	4	80
<b>Total</b>	<b>80</b>	

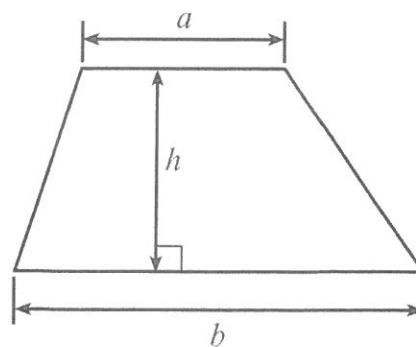
10  
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 E  
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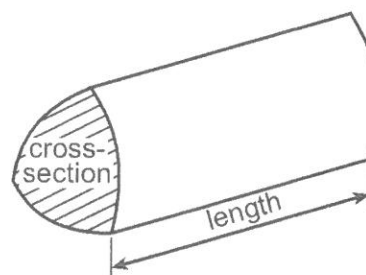
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## Formula List – Intermediate Tier

Area of trapezium =  $\frac{1}{2} (a + b)h$



Volume of prism = area of cross-section  $\times$  length



1. Calculate each of the following.

(a)  $0.4 \times 0.7$

[1]

$$0.28$$

B1

(b)  $13.8 - 7.45$

[1]

$$\begin{array}{r}
 13.80 \\
 - 7.45 \\
 \hline
 6.35
 \end{array}$$

B1

(c)  $3^3 - 2^4$

[2]

$$\begin{aligned}
 3^3 &= 3 \times 3 \times 3 = 27 \\
 2^4 &= 2 \times 2 \times 2 \times 2 = 16 \\
 \hline
 &11
 \end{aligned}$$

B1

B1

3300U301  
03

(d)  $\frac{9}{10} - \frac{3}{5} \times \frac{2}{2}$

[2]

$$\frac{9}{10} - \frac{6}{10} = \frac{3}{10}$$

M1

A1



2. Circle either TRUE or FALSE for each of the following statements.

[3]

20% of 70 is the same as 70% of 20.	<input checked="" type="radio"/> TRUE	<input type="radio"/> FALSE
$\frac{1}{2}$ of $\frac{1}{8}$ is the same as $\frac{1}{8}$ of $\frac{1}{2}$	<input checked="" type="radio"/> TRUE	<input type="radio"/> FALSE
A number is halved. The answer is halved, and then this answer is halved again. This gives the same answer as dividing the original number by 6.	<input type="radio"/> TRUE	<input checked="" type="radio"/> FALSE
Dividing a number by 15 is the same as first dividing by 10 and then dividing the answer by 5.	<input type="radio"/> TRUE	<input checked="" type="radio"/> FALSE
Multiplying a number by 2.5 is the same as first multiplying by 10 and then dividing the answer by 4.	<input checked="" type="radio"/> TRUE	<input type="radio"/> FALSE

Space for working:

10% of 70 = 7

10% of 20 = 2

Choose (18)

(18)

20% of 70 = 14

70% of 20 = 14

÷2

(9)

÷6 (3)

÷2

(4.5)

$\frac{1}{2} \times \frac{1}{8} = \frac{1}{16}$

$\frac{1}{8} \times \frac{1}{2} = \frac{1}{16}$

÷2

(2.25)

Choose (30)

(30)

÷15

(2)

÷10

(3)

÷5

(3/5)

Choose (10)

(10)

×2.5

(25)

×10

(100)

÷4

(25)





$$\begin{array}{r} 16 \\ 9 \overline{)144} \\ \underline{9} \phantom{0} \\ 54 \\ \underline{45} \\ 9 \end{array}$$

3. A shop has 31 plant pots.  
Some are blue, some are yellow and the rest are red.  
There are five more blue pots than yellow pots.  
There are four times as many blue pots as there are red pots.

Calculate how many pots there are of each colour.

$$B + Y + R = 31$$

$$\begin{array}{r} 36 \\ \times 4 \\ \hline 144 \\ \hline 2 \end{array}$$

[3]

$$\begin{aligned} B &= Y + 5 \Rightarrow B - 5 = Y \\ B &= 4R \Rightarrow \frac{B}{4} = R \end{aligned}$$

$$B + B - 5 + \frac{B}{4} = 31$$

$$2B + \frac{B}{4} = 31 + 5$$

Blue

(16)

Yellow

(11)

Red

(4)

$$2B + \frac{B}{4} = 36$$

 $\times 4$ 

$$8B + B = 144$$

$$9B = 144$$

$$B = 144 \div 9$$

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05

4. (a) Write down the next two numbers in the following sequence.

[2]

33      26      19      12      5      -2  
-7      -7      -7

- (b) Simplify the expression  $+10g - 5f - 3g + 3f$

[2]

$$7g - 2f$$

- (c) Using the formula  $2T = M + 3K$ , find the value of  $K$  when  $T = 11$  and  $M = 4$ .

[2]

$$2 \times 11 = 4 + 3K$$

$$22 = 4 + 3K$$

$$22 - 4 = 3K$$

$$18 = 3K$$

$$18 \div 3 = K$$

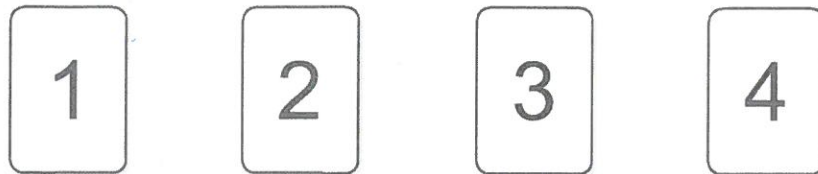
$$K = 6$$



5. Three **red** cards have the following numbers written on them.



Four **green** cards have the following numbers written on them.



In a game, the cards are turned face down.  
A player chooses one red card and one green card at random.  
The player's score is the sum of the two numbers.

- (a) Complete the following table.

[1]

		Score			
Red card	9	10	11	12	13
	6	7	8	9	10
	3	4	5	6	7
		1	2	3	4
		Green card			

- (b) A player wins a prize if the score is more than 9.  
Safira plays the game once. What is the probability that she wins a prize?

[2]

$$\frac{5}{12}$$

- (c) 60 people play the game once.  
Approximately how many people would you expect to win a prize?

[2]

$$\frac{5}{12} \times 60 = 5 \times 5 = 25$$



B1

B1  
B1M1  
A1

6. In this question, you will be assessed on the quality of your organisation, communication and accuracy in writing.

A right-angled triangle  $BCD$  is joined to a rectangle  $ABDE$ , as shown below.

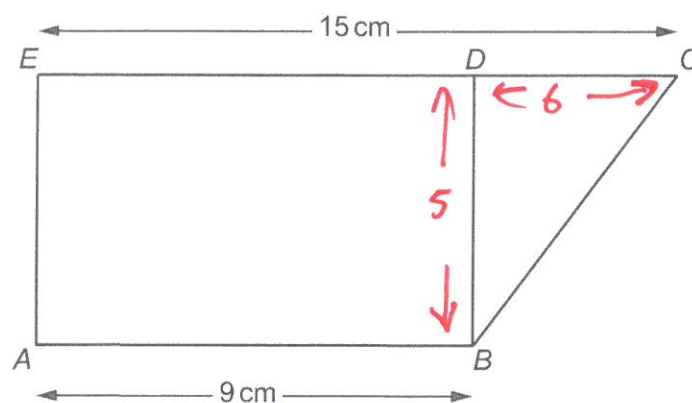


Diagram not drawn to scale

The area of the rectangle is  $45 \text{ cm}^2$ .

Calculate the area of the right-angled triangle.  
You must show your working.

[5 + 2 OCW]

$$DC = 15 - 9 = 6 \text{ cm}$$

$$\text{Need } BD: \text{ Area} = AB \times BD$$

$$9 \times BD = 45$$

$$BD = \frac{45}{9} = 5$$

$$\text{So area of } \triangle BDC = \frac{1}{2} \times 5 \times 6 = 15 \text{ cm}^2$$

B1

M1

A1

M1

A1



7. Solve each of the following equations.

(a)  $\frac{w}{5} = 10$

[1]

$$w = 10 \times 5$$

$$w = 50$$

B1

(b)  $\frac{42}{x} = 7$

[1]

$$42 = 7 \times x$$

$$\frac{42}{7} = x$$

$$x = 6$$

B1

(c)  $13y - 5 = 9y + 27$

[3]

$$13y - 5 - 9y = 27$$

$$13y - 9y = 27 + 5$$

$$4y = 32$$

$$y = \frac{32}{4} = 8$$

B1

B1

B1





8. Two types of number are added or multiplied together.  
Complete the table below to show whether the answer will be odd or even.  
One answer has been filled in for you.

[3]

Calculation:	Answer will be:
even number + even number	even
even number + odd number	odd
odd number + odd number	even
even number × even number	even
even number × odd number	even
odd number × odd number	odd

$$4 + 5 = 9$$

$$3 + 5 = 8$$

$$4 \times 6 = 24$$

$$4 \times 5 = 20$$

$$5 \times 3 = 15$$



9. Write down five numbers that satisfy all of the following conditions:

- They are all between 1 and 9 inclusive.
- ✓ They have a median value of 6.
- ✓ They have a range of 7.
- ✓ Their mean is 5.

[3]

1	3	6	7	8
---	---	---	---	---

$$\text{MEAN} = \frac{\text{TOTAL}}{5}$$

$$5 = \frac{\text{Total}}{5}$$

$$5 \times 5 = \text{Total}$$

$$\text{Total} = 25$$



10. A regular polygon has exterior angles of  $45^\circ$ .

(a) How many sides does this polygon have? [2]

$$\begin{array}{l} \text{exterior angle} = \frac{360}{n^{\circ} \text{ of sides}} \\ 45 = \frac{360}{n} \quad n = \frac{360}{45} \\ \begin{array}{r} 45 \times 7 \\ \hline 315 \end{array} \quad \begin{array}{r} 45 \times 8 \\ \hline 360 \end{array} \end{array}$$

So 8 sides.

(b) Each side of this regular polygon is 7 cm.  
A sketch of two sides, AB and BC, of the polygon is shown below.

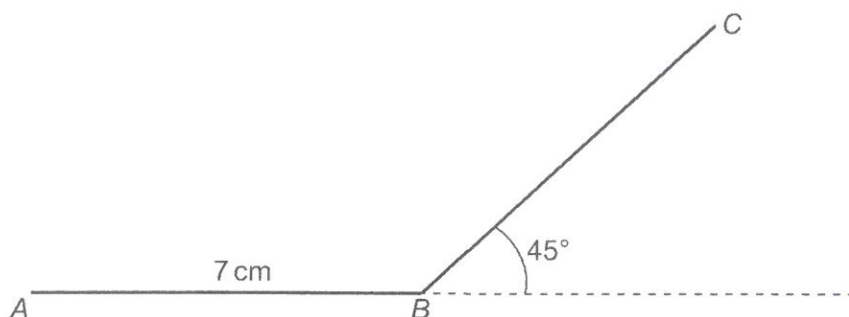
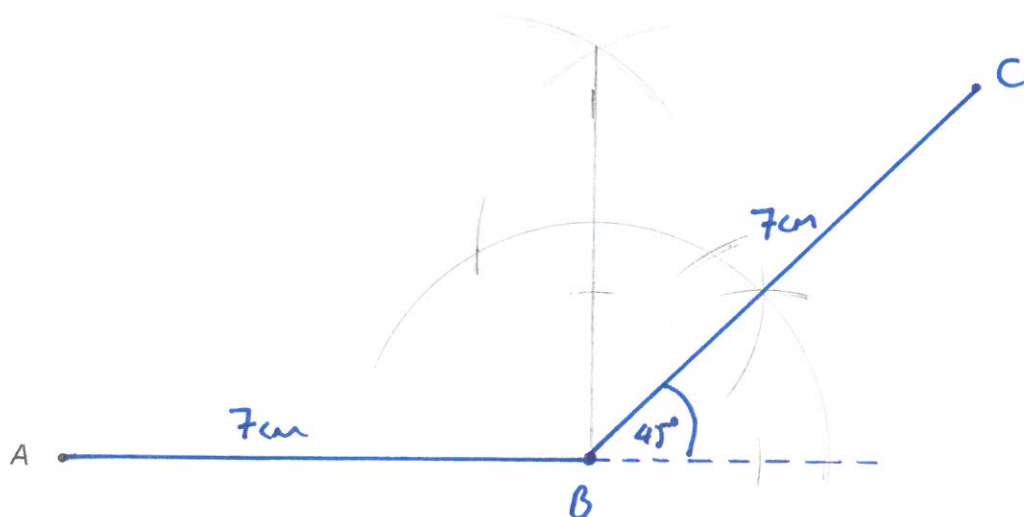


Diagram not drawn to scale

Using only a ruler and a pair of compasses, construct an accurate drawing that shows these **two sides** of the polygon.

The point A has been given.  
You must show your construction arcs. [4]



$x( )$

12

$\cup \cap$

11. (a) The table below shows some of the values of  $y = 2x^2 - 5x - 1$  for values of  $x$  from -2 to 4.

Complete the table by finding the value of  $y$  for  $x = -1$  and for  $x = 2$ .

[2]

$x$	-2	-1	0	1	2	3	4
$y = 2x^2 - 5x - 1$	17	6	-1	-4	-3	2	11

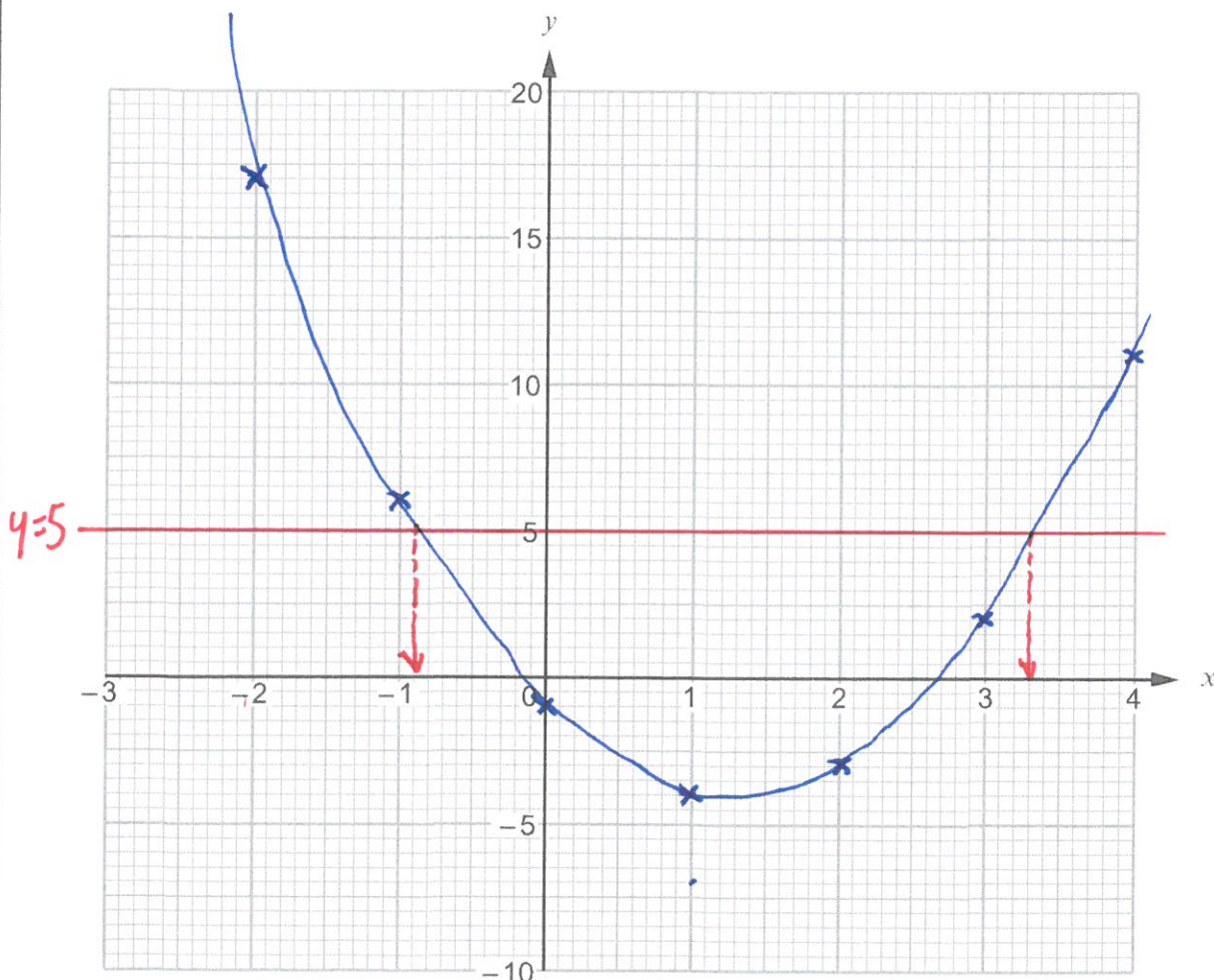
$x = -2 \quad y = 2(-2)^2 - 5(-2) - 1$   
 $= 2(4) + 10 - 1$   
 $= 8 + 10 - 1$   
 $= 17 \checkmark$

$x = -1 \quad y = 2(-1)^2 - 5(-1) - 1$   
 $= 2(1) + 5 - 1$   
 $= 2 + 5 - 1$   
 $= 6 \checkmark$

$x = 2 \quad y = 2(2)^2 - 5(2) - 1$   
 $= 8 - 10 - 1$   
 $= -3 \checkmark$

- (b) On the graph paper below, draw the graph of  $y = 2x^2 - 5x - 1$  for values of  $x$  from -2 to 4.

[2]



12



- (c) Draw the line  $y = 5$  on the graph paper.

Write down the values of  $x$  where the line  $y = 5$  cuts the curve  $y = 2x^2 - 5x - 1$ .  
Give your answers correct to 1 decimal place.

[2]

Values of  $x$  are -0.9 and 3.3

- (d) Circle the equation below whose solutions are the values you have given in (c).

[1]

$2x^2 - 5x - 1 = 0$

$2x^2 - 5x - 6 = 0$

$2x^2 - 5x - 5 = 0$

$2x^2 - x - 1 = 0$

$2x^2 - 5x + 4 = 0$

$2x^2 - 5x - 1 = 5$

$2x^2 - 5x - 1 - 5 = 0$

$2x^2 - 5x - 6 = 0$



12. A fair six-sided dice and a fair coin are thrown together once.

Circle the correct answer for each of the following statements.

(a) The number of possible outcomes is

2

6

8

12

24.

[1]

(b) The probability of getting a 4 on the dice and a tail on the coin is

 $\frac{1}{8}$  $\frac{1}{12}$  $\frac{1}{2}$  $\frac{1}{6}$  $\frac{1}{24}$ 

[1]

(c) The probability of getting a multiple of 3 on the dice and a head on the coin is

 $\frac{1}{8}$  $\frac{1}{12}$  $\frac{1}{2}$  $\frac{1}{6}$  $\frac{1}{24}$ 

[1]

Space for working:

<u>Dice</u>	<u>Coin</u>	<u>on</u>	<u>Dice</u>	<u>coin</u>
1	H		1	T
2	H		2	T
3	H		3	T
4	H		4	T
5	H		5	T
6	H		6	T

$$\frac{2}{12} = \frac{1}{6}$$



13. (a) Make  $m$  the subject of the formula  $y = 6m + 7$ . [2]

$$y - 7 = 6m$$

$$\frac{y - 7}{6} = m$$

- (b) Factorise  $6x^2 - 12x$ . [2]

$$\cancel{6}x^2 - \cancel{6} \times 2 \times x$$

$$6x(x - 2)$$

14. Find, in standard form, the value of each of the following.

(a)  $\frac{7.5 \times 10^6}{5000}$  [2]

$$\frac{7.5 \times 10^6}{5 \times 10^3} = (7.5 \div 5) \times (10^6 \div 10^3)$$

$$1.5 \times 10^3$$

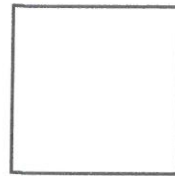
(b)  $(2.3 \times 10^3) + (6.4 \times 10^4)$  [2]

$$6.63 \times 10^4$$

$10^6$	$10^5$	$10^4$	$10^3$	$10^2$	$10^1$	$10^0$
		5	0	0	0	0
		2	3	0	0	0
		6	4	0	0	0
		6	6	3	0	0

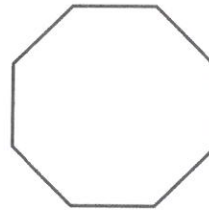


15. Each side of a square is of length  $(2x + 3y)$  cm.  
The perimeter of the square is 62 cm.



$(2x + 3y)$  cm

Each side of a regular octagon is of length  $(x + 2y)$  cm.  
The perimeter of the octagon is 72 cm.



$(x + 2y)$  cm

Use an algebraic method to find the value of  $x$  and the value of  $y$ .

[5]

For square,  $4(2x + 3y) = 62 \Rightarrow 2x + 3y = 15.5$  — (1)  
for octagon,  $8(x + 2y) = 72 \Rightarrow x + 2y = 9$  — (2)

$2x + 3y = 15.5$  — (1)

(2)  $\times 2$   $2x + 4y = 18$  — (3)

(3)  $-$  (1)  $y = 2.5$

Substitute in (2)  $x + 2 \times 2.5 = 9$

$x + 5 = 9$

$x = 9 - 5$

$x = 4$

$x = 4$   $y = 2.5$





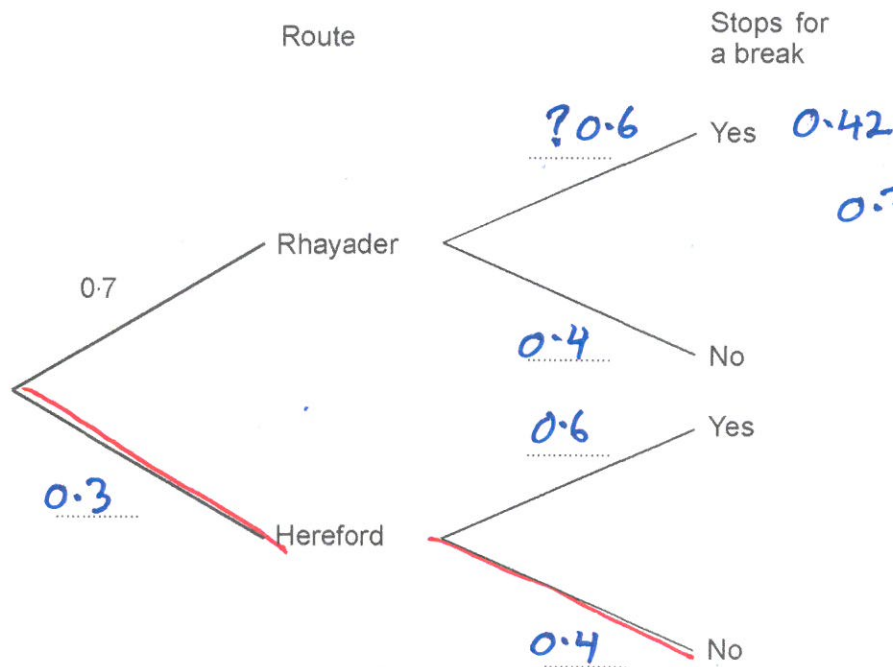
16. Alwyn often drives from Bangor to Cardiff.  
He always chooses one of two routes for these journeys.  
He either travels through Rhayader or through Hereford.  
The probability that he travels through Rhayader is 0.7.

Sometimes he decides to stop for a break during his journey.  
His decision is independent of the route he takes.

The probability that he travels through Rhayader and stops for a break is 0.42.

- (a) Complete the following tree diagram.

[4]



- (b) Calculate the probability that Alwyn travels through Hereford but **does not** stop for a break. [2]

$$0.3 \times 0.4 = 0.12$$



17. William has  $n$  marbles.

Lois had 4 times as many marbles as William, but she has now lost 23 of them.

Lois still has more marbles than William.

Write down an inequality in terms of  $n$  to show the above information.

Use your inequality to find the least number of marbles that William may have.

[4]

$$4n - 23 > n$$

$$4n > n + 23$$

$$4n - n > 23$$

$$3n > 23$$

$$n > \frac{23}{3}$$

$$n > 7\frac{2}{3}$$

$$\text{So } n = 8$$

END OF PAPER

B1B1

B1

B1









GCSE MATHEMATICS Unit 1 : Intermediate Tier Autumn 2016		✓	Mark	Comment														
8 <table border="1"><thead><tr><th>Sum</th><th>Answer</th></tr></thead><tbody><tr><td>even + even</td><td>(even)</td></tr><tr><td>even + odd</td><td>odd</td></tr><tr><td>odd + odd</td><td>even</td></tr><tr><td>even × even</td><td>even</td></tr><tr><td>even × odd</td><td>even</td></tr><tr><td>odd × odd</td><td>odd</td></tr></tbody></table>		Sum	Answer	even + even	(even)	even + odd	odd	odd + odd	even	even × even	even	even × odd	even	odd × odd	odd		B3	For all 5 correct. B2 for 4 correct. B1 for 3 correct. B0 for fewer than three correct.
Sum	Answer																	
even + even	(even)																	
even + odd	odd																	
odd + odd	even																	
even × even	even																	
even × odd	even																	
odd × odd	odd																	
9. All four conditions met. <ul style="list-style-type: none"><li>• All numbers between 1 and 9 inclusive.</li><li>• Median value = 6</li><li>• Range = 7</li><li>• Total = 25</li></ul>			B3	B2 for three conditions met. B1 for two conditions met. Possible answers for B3 are 1, 2, 6, 8, 8. OR 1, 3, 6, 7, 8. OR 1, 4, 6, 6, 8. OR 2, 2, 6, 6, 9. Must have five numbers, otherwise B0. Numbers need not be integers. Numbers shown in the boxes take precedence. If answer boxes are left blank allow <u>unambiguous</u> indication of their <u>five</u> numbers.														
10. (a) $\frac{360}{45}$  = 8 (sides)			M1  A1	For a clear intention of finding how many 45s in 360. Accept embedded answers e.g. $360/8 = 45$ or $45 \times 8 = 360$ for M1A1.														
10.(b)  Correct construction of 90°.     Correct bisector of 90°.   AB = 7cm    AND    BC = 7cm			B2          B1    B1	Do not penalise if they use their own point A. <u>Use overlay</u> but arcs required for the 3 'angle marks'. With sight of accurate 'method arcs'. For this B2 the construction need not be at point B. (Final B1 will not then be awarded) B1 for sight of 'method arcs' but perpendicular line not drawn (Unless intersection of construction arcs for 90° are correctly used to construct the 45° angle. In this case the B2 and B1 are gained)  With sight of accurate 'method arcs'. F.T. 'their 90°'.  Allow ± 0.2cm. Do not penalise if the line AB is extended as long as the position of point B is unambiguous. (Allow labelling of points B and C to be missing if end points are unambiguously identifiable.) <i>If <u>all</u> marks gained but angle ABC = 45°, penalise -1.</i>														



GCSE MATHEMATICS Unit 1 : Intermediate Tier Autumn 2016	✓	Mark	Comment
15. (Perimeter of square =) $4 \times (2x + 3y) = 62$	✓	B1	Sight of $8x + 12y = 62$ or equivalent e.g. $2x + 3y = 15.5$
(Perimeter of octagon =) $8 \times (x + 2y) = 72$	✓	B1	Sight of $8x + 16y = 72$ or equivalent e.g. $x + 2y = 9$
Correct method to solve simultaneous equations, as far as attempt at subtraction	✓	M1	F.T. 'their equations'. Allow 1 'slip', if multiplication used, but not in 'equated variable' for M1 <u>only</u> .
$y = 2.5$	✓	A1	
$x = 4$	✓	A1	F.T. from their 1 <sup>st</sup> variable. (Substitution in any relevant equation.)
<b>Ribbon marking for 16(a) and 16(b).</b>			
16.(a) 0.3 on 'Hereford' branch.	✓	B1	
$0.7 \times P(\text{Yes}) = 0.42$	✓	M1	Allow their notation for P(Yes).
$P(\text{Yes}) = 0.6$	✓	A1	
0.6, 0.4, 0.6 and 0.4 correctly placed.	✓	A1	F.T. 'their P(Yes)', if between 0 and 1 but not 0.5.
<b>Ribbon marking for 16(a) and 16(b).</b>			
16(b) $0.3 \times 0.4$		M1	F.T. 'their values' if both between 0 and 1.
$= 0.12$		A1	
17. $4n - 23 > n$ or $n < 4n - 23$ or equivalent.	✓✓	B2	B1 for $4n \pm \dots > n$ OR B1 for $4n - 23 > an + b$ $a \neq 0$ . OR B1 for $4n - 23 \geq n$ .  B0 for $4n - 23 < n$
(least number of marbles =) 8	✓✓	B2	F.T. from 'their <u>inequality</u> ', if of equivalent difficulty. (e.g. $4n - 23 > n + 23$ giving an answer of 16)  B1 for sight of $n > \frac{23}{3}$ or equivalent. (With similar F.T. answer e.g. $n > 46/3$ from above example of $4n - 23 > n + 23$ )  OR allow B1 for $n > 7$ OR $n \geq 8$ (With similar F.T. answer e.g. $n > 15$ from above example of $4n - 23 > n + 23$ )